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# Comment

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#### 1. INTRODUCTION

The paper by Kleibergen and Mavroeidis (2009), hereafter KM, is an excellent survey of the current state of the art in the weak instrument robust econometrics for testing subsets of parameters in the generalized method of moments (GMM), and provides an important and relevant application of the econometric theory to the analysis of the new Keynesian Phillips curve. We are extremely grateful to have the opportunity to comment on this very nice paper. Our comments will focus on the weak instrument robust tests for subsets of parameters, and in particular on the projection-based test that KM refer to as the Robins (2004) test.

We show that KM's implementation of the Robins test is inefficient, and provide an efficient implementation that performs nearly as well as the MQLR test recommended by KM. Our comment proceeds as follows. Section 2 reviews the tests used for inference on subsets of parameters in GMM and discusses in detail the implementation of the Robins test, which we call the new method of projection. Section 3 reports the results of a small simulation study to demonstrate that the new method of projection performs nearly as well as the tests recommended by KM. Section 4 contains our concluding remarks.

## 2. INFERENCE ON SUBSETS OF PARAMETERS IN GMM

In this section we describe inference on subsets of parameters in the GMM framework. We follow the notation and assumptions of KM regarding the GMM framework. Interest centers on a *p*-dimensional vector of parameters  $\theta$  identified by a set of  $k \ge p$  moment conditions

$$E[f_t(\theta)] = 0.$$

Let  $\theta = (\alpha', \beta')'$ , where  $\alpha$  is  $p_{\alpha} \times 1$  and  $\beta$  is  $p_{\beta} \times 1$ . The parameters of interest are  $\beta$ , and  $\alpha$  are considered nuisance parameters. The weak identification robust methods of inference on

 $\theta$  are based on the (efficient) continuous updating (CU) GMM objective function

$$Q(\theta) = T f_T(\theta)' \hat{V}_{ff}(\theta)^{-1} f_T(\theta), \qquad (1)$$

where  $f_T(\theta) = T^{-1} \sum_{t=1}^T f_t(\theta)$  and  $\hat{V}_{ff}(\theta)$  is a consistent estimator of the  $k \times k$  dimensional covariance matrix  $V_{ff}(\theta)$  of the vector of sample moments. Let  $q_t(\theta) = \text{vec}(\frac{\partial f_t(\theta)}{\partial \theta'})$  and define  $\bar{f}_t(\theta) = f_t(\theta) - E[f_t(\theta)]$  and  $\bar{q}_t(\theta) = q_t(\theta) - E[q_t(\theta)]$ . Assumption 1 of KM states that

$$\frac{1}{\sqrt{T}} \sum_{t=1}^{T} \begin{bmatrix} \bar{f}_t(\theta) \\ \bar{q}_t(\theta) \end{bmatrix} \stackrel{d}{\to} \begin{bmatrix} \psi_f(\theta) \\ \psi_\theta(\theta) \end{bmatrix} \sim \mathcal{N}(0, V(\theta)).$$
$$V(\theta) = \begin{bmatrix} V_{ff}(\theta) & V_{f\theta}(\theta) \\ V_{\theta f}(\theta) & V_{\theta \theta}(\theta) \end{bmatrix}.$$

The gradient of (1) with respect to  $\theta$  is given by

$$\nabla_{\theta} Q(\theta) = \frac{\partial Q(\theta)}{\partial \theta'} = 2f_T(\theta)' \hat{V}_{ff}(\theta)^{-1} \hat{D}_T(\theta)$$

where  $\hat{D}_T(\theta) = \sum_{t=1}^T D_t(\theta)$  and  $D_t(\theta) = \text{devec}_k[q_t(\theta) - \hat{V}_{\theta f}(\theta)\hat{V}_{f f}(\theta)^{-1}f_t(\theta)]$ . For the definition of the devec operator see Chaudhuri (2008).

#### 2.1 Tests for the Full Parameter Vector

Valid tests of the hypothesis  $H_0: \theta = \theta_0$  were developed in Stock and Wright (2000) and Kleibergen (2005). Stock and Wright's S-statistic is a generalization of the Anderson–Rubin statistic (see Anderson and Rubin 1949) and is given by  $S(\theta) = Q(\theta)$ . Kleibergen's K-statistic is a score-type statistic based on  $Q(\theta)$  and may be expressed as

$$K(\theta) = \frac{1}{4} (\nabla_{\theta} Q(\theta)) [\hat{D}_T(\theta)' \hat{V}_{ff}(\theta)^{-1} \hat{D}_T(\theta)]^{-1} (\nabla_{\theta} Q(\theta))'.$$
(2)

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Under the null 
$$H_0: \theta = \theta_0$$
,  $S(\theta_0) \stackrel{A}{\sim} \chi_k^2$  and  $K(\theta_0) \stackrel{A}{\sim} \chi_p^2$ 

#### 2.2 Tests for Subsets of Parameters

For testing hypotheses on subsets of parameters of the form  $H_0: \beta = \beta_0$ , subset versions of the S- and K-statistics were also considered by Stock and Wright (2000) and Kleibergen (2005). These statistics are based on the plug-in principle and utilize the constrained CU-GMM estimate  $\tilde{\alpha}(\beta_0) = \arg \min_{\alpha} Q(\alpha, \beta_0)$ . Letting  $\tilde{\theta}_0 = (\tilde{\alpha}(\beta_0)', \beta_0')'$ , the subset S- and K-statistics are given by  $S(\tilde{\theta}_0)$  and  $K(\tilde{\theta}_0)$ , respectively. Under the null  $H_0: \beta =$  $\beta_0$  and under the assumption that  $\alpha$  is well identified, Stock and Wright (2000) and Kleibergen (2005) showed that  $S(\tilde{\theta}_0) \sim^A$  $\chi^2_{k-p_{\alpha}}$  and  $K(\tilde{\theta}_0) \stackrel{A}{\sim} \chi^2_{p_{\beta}}$ . This result is based on the fact that when  $\alpha$  is well identified,  $\tilde{\alpha}(\beta_0)$  is  $\sqrt{n}$  consistent for  $\alpha$  under  $H_0: \beta = \beta_0$ . When  $\alpha$  is not well identified,  $\tilde{\alpha}(\beta_0)$  is no longer  $\sqrt{n}$  consistent for  $\alpha$  and hence the S- and K-statistics are not asymptotically chi-square distributed. However, Theorem 1 of KM shows that irrespective of the identification of  $\alpha$ , the S- and *K*-statistics are always bounded from above by the  $\chi^2_{k-p_{\alpha}}$  and  $\chi^2_{p_{\beta}}$  distributions, respectively.

#### 2.3 Usual Method of Projection

Dufour (1997), Dufour and Jasiak (2001), and Dufour and Taamouti (2005, 2007) showed that the usual projection approach could always be used to obtain valid inference for subsets of parameters provided there exists an asymptotically (boundedly) pivotal statistic for testing the joint hypothesis  $H_0: \theta = \theta_0$ . Let  $R(\theta)$  denote such a statistic and assume that  $R(\theta) \stackrel{A}{\sim} \chi_v^2$ . Suitable choices for  $R(\theta)$  are  $S(\theta)$ , for which v = k, and  $K(\theta)$ , for which v = p. The usual method of projection rejects  $H_0: \beta = \beta_0$  at level (at most)  $\zeta$  if

$$\inf_{\alpha\in\Theta_{\alpha}}R(\alpha,\beta_0)>\chi_{\nu}^2(1-\zeta)$$

where  $\Theta_{\alpha}$  denotes the parameter space for  $\alpha$ , and  $\chi_{\nu}^{2}(1-\zeta)$  denotes the  $1-\zeta$  quantile of the chi-square distribution with  $\nu$  degrees of freedom. The asymptotic size of the projection test cannot exceed  $\zeta$  irrespective of the identification of  $\alpha$  or  $\beta$  or both. However, the power of the test can be very low if  $\nu$  is large compared to  $p_{\beta}$ .

#### 2.4 New Method of Projection

Chaudhuri et al. (2007), Chaudhuri (2008), and Chaudhuri and Zivot (2008) proposed a new method of projection for making inferences on subsets of parameters in the presence of potentially unidentified nuisance parameters that are based on ideas presented in Robins (2004). The new method of projection requires (i) a uniform asymptotic  $(1 - \xi) \cdot 100\%$  confidence set,  $C_{\alpha}(1 - \xi, \beta_0)$ , for  $\alpha$  when the null hypothesis  $H_0 : \beta = \beta_0$ is true, and (ii) an asymptotically pivotal statistic  $R(\theta)$ . In most cases, as described in Table 1,  $R(\theta) \stackrel{A}{\sim} \chi_{\nu}^2$  for some  $\nu$  depending upon the choice of  $R(\theta)$ .

Then the new method of projection rejects  $H_0: \beta = \beta_0$  if

(1) 
$$C_{\alpha}(1-\xi,\beta_0) = \emptyset$$
, or

Table 1. Confidence sets, test statistics, and degrees of freedom for new-projection-type tests

$\overline{C_{\alpha}(1-\xi,\beta_0)}$	$R(\alpha, \beta)$	v
$C_{\alpha}^{K}(1-\xi,\beta_{0})$	$S(\alpha, \beta_0)$	k
$C_{\alpha}^{K}(1-\xi,\beta_{0})$	$K(\alpha, \beta_0)$	р
$C_{\alpha}^{K_{\alpha}}(1-\xi,\beta_0)$	$K_{\beta.lpha}(lpha, eta_0)$	Pβ
$C^S_{\alpha}(1-\xi,\beta_0)$	$S(\alpha, \beta_0)$	k
$C^S_{\alpha}(1-\xi,\beta_0)$	$K(\alpha, \beta_0)$	р
$C^S_{\alpha}(1-\xi,\beta_0)$	$K_{\beta.lpha}(lpha,eta_0)$	pβ

(2)  $\inf_{\alpha_0 \in C_{\alpha}(1-\xi,\beta_0)} R(\alpha_0,\beta_0) > \chi_v^2(1-\zeta).$ 

Under the null hypothesis  $H_0: \beta = \beta_0$ ,  $C_\alpha(1 - \xi, \beta_0)$  asymptotically contains  $\alpha$  with probability at least  $1 - \xi$ , and hence it follows from Bonferroni's inequality that the asymptotic size of the new projection type test cannot exceed  $\zeta + \xi$ . The new method of projection can be expected to be generally less conservative than the usual method of projection because the infimum for the new method is only computed over  $C_\alpha(1 - \xi, \beta_0)$ , whereas the infimum is computed over the whole space  $\Theta_\alpha$  for the usual method. Similar projection methods have also been employed by Dufour (1990), Berger and Boos (1994), and Silvapulle (1996).

To implement the new method of projection in the context of GMM,  $C_{\alpha}(1 - \xi, \beta_0)$  can be constructed by inverting the *S*- or *K*-tests as

$$C_{\alpha}^{S}(1-\xi,\beta_{0}) = \{\alpha : S(\alpha,\beta_{0}) \le \chi_{k}^{2}(1-\xi)\} \quad \text{or} \\ C_{\alpha}^{K}(1-\xi,\beta_{0}) = \{\alpha : K(\alpha,\beta_{0}) \le \chi_{p}^{2}(1-\xi)\}.$$

An advantage of using  $C_{\alpha}^{K}(1 - \xi, \beta_{0})$  is that it will never be empty, and the asymptotic properties of the test will only depend on  $R(\theta)$  when  $\alpha$  is well identified. However, it will also include saddlepoints  $\alpha^{*}$  where  $K(\alpha^{*}, \beta_{0}) = 0$  and these points are associated with spurious declines in power of the *K*-statistic. In contrast, the set  $C_{\alpha}^{S}(1 - \xi, \beta_{0})$  can be empty and this will occur for values  $\beta_{0}$  at which the overidentifying restrictions are rejected (at level  $\xi$ ). As we show in the next section, this can lead to improved power properties of the new method of projection.

While the new method of projection can be implemented using any asymptotically pivotal statistic  $R(\theta)$ , Robins (2004) showed that there are certain advantages of using an efficient score-type statistic for  $R(\theta)$ . The efficient score for  $\beta$  (given  $\alpha$ ), in the terminology of van der Vaart (1998), is the part of the score (gradient of the objective function with respect to) for  $\beta$ that is orthogonal to the score for  $\alpha$ . The efficient score statistic for  $\beta$  is a quadratic form in the efficient score for  $\beta$  with respect to an estimator of its asymptotic variance. In the context of GMM, Chaudhuri (2008) and Chaudhuri and Zivot (2008) decomposed the *K*-statistic (2) into two orthogonal statistics: a *K*-statistic for  $\alpha$  (given  $\beta$  known) and an efficient (score) *K*statistic for  $\beta$ 

$$K(\theta) = K_{\alpha}(\theta) + K_{\beta,\alpha}(\theta),$$

The data-generating process is

$$K_{\alpha}(\theta) = \frac{1}{4} (\nabla_{\alpha} Q(\theta)) (\hat{D}_{T\alpha}(\theta)' \hat{V}_{ff}(\theta)^{-1/2} \hat{D}_{T\alpha}(\theta))^{-1} \\ \times (\nabla_{\alpha} Q(\theta))',$$
  
$$K_{\beta,\alpha}(\theta) = \frac{1}{4} (\nabla_{\beta,\alpha} Q(\theta)) (\hat{D}_{T\beta}(\theta)' \hat{V}_{ff}(\theta)^{-1/2} N_{\hat{V}_{ff}(\theta)^{-1/2} \hat{D}_{T\alpha}(\theta)} \\ \times \hat{V}_{ff}(\theta)^{-1/2} \hat{D}_{T\beta}(\theta))^{-1} (\nabla_{\beta,\alpha} Q(\theta))',$$

and  $\nabla_{\beta,\alpha}Q(\theta)$  is the estimated efficient score for  $\beta$  defined as

$$\nabla_{\beta,\alpha} \mathcal{Q}(\theta) = f_T(\theta)' \hat{V}_{ff}(\theta)^{-1/2} \\ \times N_{\hat{V}_{ff}(\theta)^{-1/2'} \hat{D}_{T\alpha}(\theta)} \hat{V}_{ff}(\theta)^{-1/2} \hat{D}_{T\beta}(\theta).$$

The above expressions use the partition  $\hat{D}_T(\theta) = [\hat{D}_{T\alpha}(\theta), \hat{D}_{T\beta}(\theta)]$  and  $\hat{V}_{\theta f} = [\hat{V}_{\alpha f}(\theta)', \hat{V}_{\beta f}(\theta)']'$ .

It can be shown that under  $H_0: \theta = \theta_0$ ,  $K_\alpha(\theta_0) \stackrel{A}{\sim} \chi^2_{p_\alpha}$ and  $K_{\beta,\alpha}(\theta_0) \stackrel{A}{\sim} \chi^2_{p_\beta}$ . Furthermore, if  $\theta_0$  belongs to the  $\sqrt{n}$ neighborhood of  $\theta$ , then  $K_{\beta,\alpha}(\theta_0) = K_{\beta,\alpha}(\theta) + o_p(1)$ . This latter property of  $K_{\beta,\alpha}(\theta)$  makes it ideally suited for use in the new method of projection. Indeed, Chaudhuri (2008) proved that if  $C_\alpha(1 - \xi, \beta_0)$  is nonempty with probability approaching one and if  $\alpha$  is well identified then the newmethod-of-projection-type test that rejects  $H_0: \beta = \beta_0$  when  $\inf_{\alpha_0 \in C_\alpha(1-\xi,\beta_0)} K_{\beta,\alpha}(\theta_0) > \chi^2_{p_\beta}(1-\zeta)$  is asymptotically equivalent to the size (at most)  $\zeta$  *K*-test for  $\beta$  against local alternatives. This means that the new method of projection with  $R(\theta) = K_{\beta,\alpha}(\theta)$  is size controlled when  $\alpha$  is not identified and can be made asymptotically equivalent to Kleibergen's *K*-test when  $\alpha$  is well identified.

Table 1 summarizes the possible ways of implementing the new-method-of-projection-type tests for testing  $H_0: \beta = \beta_0$ . KM illustrated the use of the new method of projection with  $C_{\alpha}(1-\xi,\beta_0) = C_{\alpha}^K(1-\xi,\beta_0)$  and  $R(\theta) = S(\alpha,\beta_0)$  and concluded that the Robins test, proposed in Chaudhuri (2008) and Chaudhuri et al. (2007), does not outperform the usual method of projection based on  $R(\theta) = S(\alpha, \beta_0)$ . However, this is not what Chaudhuri (2008) and Chaudhuri et al. (2007) refer to as the Robins test. In the context of GMM, Chaudhuri (2008) and Chaudhuri and Zivot (2008) recommend using  $C_{\alpha}(1-\xi,\beta) =$  $C^{S}_{\alpha}(1-\xi,\beta)$  and  $R(\theta) = K_{\beta,\alpha}(\theta)$ . The power of this method is largely driven by the choice of the statistic  $R(\theta)$ . In addition, the choice  $R(\theta) = K_{\beta,\alpha}(\theta)$  (i.e., the efficient K-statistic) can make this test asymptotically equivalent the K-test when  $\alpha$ is well identified. In the next section we show, using the same simulation experiment as KM, that this latter implementation of the new method of projection performs comparably to the tests recommended by KM.

#### 3. SIMULATIONS

To illustrate the finite sample properties of the new method of projection based on  $C_{\alpha}^{S}(1-\xi,\beta_{0})$  and  $K_{\beta,\alpha}(\alpha,\beta_{0})$  we utilize the same simulation experiment described in Section 4 of KM. We are grateful to Frank Kleibergen and Sophocles Mavroeidis for sharing their Matlab code with us.

$$\pi_{t} = \lambda x_{t} + \gamma_{f} E_{t}[\pi_{t+1}] + u_{t},$$
  

$$x_{t} = \rho_{1} x_{t-1} + \rho_{2} x_{t-2} + v_{t},$$
  

$$\pi_{t+1} = (\alpha_{0} \rho_{1} + \alpha_{1}) x_{t} + \alpha_{0} \rho_{2} x_{t-1} + \eta_{t+1}$$

where  $\eta_t = u_t + \alpha_0 v_t$ . There error terms  $\eta_t$  and  $v_t$  are jointly normal with unit variances and correlation  $\rho_{\eta v} = 0.2$ . The parameter of interest is  $\gamma_f$  and  $\lambda$  is the nuisance parameter. Identification of the structural parameters  $\lambda$  and  $\gamma_f$  is controlled by the concentration parameter  $\mu^2$ , which is a complicated nonlinear function of the model parameters.

KM's Figure 3 illustrates the power curves for testing  $H_0: \gamma_f = 1/2$  against  $H_1: \gamma_f \neq 1/2$  at the 5% level for the subset *S*, usual method of projection based on *S*, and the new method of projection based on  $C_{\lambda}^K(1 - \xi, \gamma_f = 1/2)$  and  $S(\lambda, \gamma_f = 1/2)$  with  $\xi = 0.02$  and  $\zeta = 0.03$ . The figure shows that the power curves of the usual method of projection and an inefficient application of the new method are indistinguishable and are dominated by the subset *S*-statistic.

Figure 1 in this note shows the power curves of the new method of projection based on  $C_{\lambda}^{S}(1 - \xi, \gamma_{f} = 1/2)$  and  $K_{\lambda,\gamma_{f}}(\lambda, \gamma_{f} = 1/2)$  with  $\xi = 0.005$  and  $\zeta = 0.045, 0.05$ , along with the recommended tests of KM. The graphs show that the new method of projection actually performs as well as the MQLR and KJ tests recommended by KM. For the strong identification case, use of  $C_{\lambda}^{S}(1 - \xi, \gamma_{f} = 1/2)$  avoids the spurious decline in power observed for the KLM statistic.

#### 4. CONCLUSION

KM show that the subset versions of the S, K, and MQLR statistics are valid tests even when the nuisance parameters are unidentified. This is an important theoretical and practical result. Their simulation results calibrated to a stylized new Keynesian Phillips curve show that projection-type tests are too conservative and are dominated by the subset S, K, and MQLR statistics. We show that a version of the Robins test, which we call the new method of projection, based on an efficient score-type statistic performs nearly as well as the MQLR statistic and provides an alternative approach to weak instrument robust inference for subsets of parameters in models estimated by GMM.

A practical drawback of the weak instrument robust tests is that they are based on the CU-GMM objective function. The CU-objective function can be ill-behaved, even for linear models, and finding the global minimum can be difficult. Moreover, most commercial software implementations of GMM do not support CU-GMM. Until commonly used software implementations of GMM catch up with the important theoretical developments surveyed by KM, it is not likely that weak instrument robust methods will be widely used in practice.

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where



Figure 1. Power curves of 5% level tests for  $H_0: \gamma_f = 0.5$  against  $H_1: \gamma_f \neq 0.5$ . The sample size is 1,000 and the number of Monte Carlo simulations is 10,000.

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# Rejoinder

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# 1. INTRODUCTION

We would like to thank Fabio Canova, Saraswata Chaudhuri, John Chao, Jean-Marie Dufour, Anna Mikusheva, Norman Swanson, Jonathan Wright, Moto Yogo, and Eric Zivot for their stimulating discussions of our article. We especially like the diversity of the different discussions, which caused them to have hardly any overlap while all of them provide insightful comments from the discussant's own research perspective. Because of the small overlap of the different discussions, we comment on them separately and do so in alphabetical order.

#### 2. CANOVA

In his discussion, Canova brings up the issue of the structural versus semistructural specifications of the model. Indeed, we received similar comments when we presented the article at the Joint Statistical Meetings (JSM) conference in Denver, so we revised the article somewhat to give results for a particular structural specification proposed by Galí and Gertler (1999).